

Reg. No. : .....

Name : .....

**Third Semester B.Sc. Degree Examination, October 2019**

**First Degree Programme Under CBCSS**

**Complementary Course for Physics**

**ST 1331.2 : PROBABILITY DISTRIBUTIONS AND STOCHASTIC PROCESS**

**(2017 Admission onwards)**

Time : 3 Hours

Max. Marks : 80

Use of Calculator and Statistical table is permitted.

**SECTION – A**

Answer all questions. Each question carries 1 mark.

1. Define uniform distribution in continuous case.
2. Write down the mean and variance of a binomial distribution with parameters  $n$  and  $p$ .
3. Name the discrete distribution which possesses lack of memory property.
4. Define statistic.
5. Name the distribution of square of a standard normal variate.
6. Define 't' distribution.
7. Write the relationship between chi square and F variates.
8. State Central Limit Theorem.

9. Define transition probability matrix.

10. Define ordered samples.

(10 × 1 = 10 Marks)

### SECTION – B

Answer any **eight** questions. Each question carries **2** marks.

11. Explain the term parameter with an example.

12. Find the distribution function of an exponential distribution.

13. Find the pdf of  $Y = -2 \log_e X$  if  $X \sim U(0, 1)$ .

14. Define Gamma distribution.

15. Write any four properties of Normal Distribution.

16. Find  $P(|X - 26| \geq 2)$  if  $X$  is a Normal variate with mean 26 and standard deviation 3.

17. Define stochastic process.

18. Explain multiplets.

19. Define F statistic and its uses.

20. Explain Maxwell – Boltzmann statistic.

21. Define sampling distribution with examples.

22. Define Brownian Motion process.

(8 × 2 = 16 Marks)

### SECTION – C

Answer any **six** questions. **Each** question carries **4** marks.

23. Show that Poisson distribution is the limiting form of Binomial.
24. State and prove the additive property of chi square distribution.
25. Obtain moment generating function of a binomial distribution.
26. Find the mean deviation about mean of  $N(\mu, \sigma^2)$ .
27. Write down the interrelationships between normal, chi square,  $t$  and  $F$  statistics.
28. If  $(X_1, X_2, X_3, X_4)$  is a random sample from  $N(0, 1)$ , find the value of  $C$  such that 
$$P\left[\frac{3X_3^2}{X_1^2 + X_2^2 + X_4^2} > C\right] = 0.01.$$
29. If  $X_1$  and  $X_2$  are two i.i.d. normal variates with mean  $\mu$  and variance  $\sigma^2$ , find the m.g.f. of  $Y = 2X_1 + 3X_2$  and identify the distribution.
30. State the postulates of Poisson process.
31. Define a process with independent increments. Give an example.

**(6 × 4 = 24 Marks)**

### SECTION – D

Answer any **two** questions. **Each** question carries **15** marks.

32. For a normally distributed population, 7% of the items have their values less than 35 and 89% have their values less than 63. Find the mean and standard deviation of the distribution.
33. The following table gives the number of accidents occurred in a certain part of a city for a period of 100 days. Fit an appropriate distribution to the data and find the expected frequencies.

X	0	1	2	3	4	5	6	7
f	25	18	13	9	4	3	2	1

34. (a) Obtain the sampling distribution of mean of a random sample from a normal distribution.
- (b) A sample of size 16 is taken from a normal population with mean 1 and standard deviation 1.5.

Find the probability that the sample mean is positive.

35. (a) Define persistent and transient states.
- (b) Show that in an irreducible Markov Chain, all states are either persistent or transient.

(2 × 15 = 30 Marks)