

Reg. No. :

Name :

First Semester M.Sc. Degree Examination, February 2025

Physics/Physics with Specialization in Nano Science/Physics with
Specialization in Space Physics

PH 212/PHNS 512/PHSP 512 : MATHEMATICAL/PHYSICS

(2020 Admission Onwards)

Time : 3 Hours

Max. Marks : 75

PART – A

Answer any **five** questions. Each question carries **3** marks.

1. Verify whether eigen values of the matrix $\begin{pmatrix} 1 & 2 & 0 \\ 2 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$ are in the disc $|\lambda - 1| \leq 2$.
2. When will the matrices $\begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$ and $\begin{pmatrix} a & 0 \\ 0 & b \end{pmatrix}$ commutes under multiplication. Verify.
3. What is the projection of a vector $\vec{a} = 2\hat{x} - 3\hat{y} + 6\hat{z}$ on vector $\vec{b} = \hat{x} - 3\hat{y} + 5\hat{z}$?
4. If $f(z) = (x^2 + ay^2) + ibxy$ is a complex analytic function of $z = x + iy$, what are the values of a and b .
5. What is the Laplace transform $f(t) = t^2$?

P.T.O.



6. Solve the differential equation $\frac{dy}{dx} = \frac{y}{x}$.
7. Why a set of matrices under multiplication do not make Abelian group.
8. Define contravariant and covariant tensors with examples.
- (5 × 3 = 15 Marks)**

PART – B

Answer **three** questions each question carries **15** marks.

9. (a) Given the eigen values $\lambda_1 = 1, \lambda_2 = -1$ and corresponding eigen values $f_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}, g_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 1 \end{pmatrix}, f_2 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$ and $g_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ -1 \end{pmatrix}$ Construct A and verify $Af_n = \lambda_n g_n$ and $Ag_n = \lambda_n f_n$.
- (b) In the spherical polar coordinate system, $q_1 = r, q_2 = \theta, q_3 = \varphi$. The transformation equations are $x = r \sin \theta \cos \varphi, y = r \sin \theta \sin \varphi, z = r \cos \theta$. Calculate the spherical polar coordinate scale factors: $(h_r, h_\theta, h_\varphi)$.

OR

10. (a) Obtain the Fourier series of a triangular wave.
- (b) Explain different distributions in probability.
11. (a) Find the Laplace transform of
- (i) Dirac delta function.
 - (ii) $\sin(\omega_0 t)$
 - (iii) $\cos(\omega_0 t)$
- (b) Consider the differential equation $x \frac{d^2 y}{dx^2} + (1 - 2n) \frac{dy}{dx} + xy = 0$. Check whether $x^n J_n(x)$ is a solution of the differential equation.

OR



12. (a) Show that $(1 - 2xt - t^2)^{-1/2}$ is a generating function of $P_n(x)$.
 (b) Prove that following recurrence relation.
 (i) $nP_n(x) = (2n - 1)xP_n(x) - (n - 1)P_{n-1}(x)$
 (ii) $nP_n(x) = xP_n(x) - P_{n-1}(x)$
13. (a) In a 3D system, find values of
 (i) δ_{ij}
 (ii) $\delta_{ij}\epsilon_{ijk}$
- (b) What is C_{3v} , group? Obtain the group multiplication table for the same.

OR

14. (a) What do you mean by character table? Write down character table for C_{4v} group.
 (b) Define covariant tensor, if $dS^2 = g_{ij}dx^i dx^j$ is invariant, show that g_{ij} is a symmetric covariant tensor of rank 2.

(3 × 15 = 45 Marks)

PART – C

Answer any **three** questions. Each question carries **5** marks.

15. With any vector \vec{A} $\vec{A} \cdot \nabla \vec{r} = A$ verify the result in Cartesian and polar coordinates.
 16. State and prove Cauchy's integral formula.
 17. Fit a straight line using principle of least square.
 18. Find the value of $J_{n-1}(x) + J_1(x)$.
 19. Define a group, Construct a group of order 4 and justify that the group satisfy all properties of a group.
 20. Obtain the metric tensor for two dimensional plane in polar coordinates.

(3 × 5 = 15 Marks)

